# St George's Central CE Primary School and Nursery

## **Maths Calculation Policy**

At St. George's Central, children are introduced to the processes of calculation by building a sequence following a C-P-A approach. The C-P-A approach stands for Concrete - Pictorial – Abstract. This means that throughout the school, we see children using concrete equipment and pictures to support their understanding of more abstract concepts.

Over time children learn how to use *models and images*, such as Dienes, place value counters, bar models and tens frames, to support their mental and informal written methods of calculation. As children's mental methods are strengthened and refined, so too are their informal written methods. These methods become more efficient and succinct and lead to efficient written methods that can be used more generally. By the end of Year 6, children are equipped with mental and written methods that they understand and can use correctly.

When faced with a calculation, children are able to decide which method is most appropriate and have strategies to check its accuracy. They will do this by asking themselves:

- Can I do this in my head?
- Can I do this in my head using drawing or jottings?
- Do I need to use a pencil and paper procedure?

At whatever stage in their learning, and whatever method is being used, it must still be underpinned by a secure and appropriate knowledge of number facts, along with those mental skills that are needed to carry out the process and judge if it was successful.

The overall aim is that when children leave primary school they:

- have a secure knowledge of <u>number facts</u> and a good understanding of the <u>four operations</u>;
- are able to use this knowledge and understanding to <u>carry out calculations mentally</u> and to apply general strategies when using one-digit and two-digit numbers and particular strategies to special cases involving bigger numbers;
- make use of diagrams and informal notes to help record steps and part answers when using mental methods that generate more information than can be kept in their heads;
- <u>have an efficient and reliable written method of calculation</u> for each operation that children can apply with confidence when undertaking calculations that they cannot carry out mentally, which leads to a formal written method.

## **ADDITION**

## **EYFS**

Maths ELG: Automatically recall (without reference to rhymes, counting or other aids) number bonds up to 5 (including subtraction facts) and some number bonds to 10, including double facts. Verbally count beyond 20, recognising the pattern of the counting system. Compare quantities up to 10 in different contexts, recognising when one quantity is greater than, less than or the same as the other quantity. Explore and represent patterns within numbers up to 10, including evens and odds and double facts.

	Concrete	Pictorial	Abstract
Add one more to a given number	4+1=		4+1= What is one more than 4?
Add two single digit numbers to find an answer  Counting two groups out to find a total	3+2= + =		3 + 2 =
Add two single digit numbers to find an answer  Counting on from the biggest number	3 + 4 =  + = Children should be able to make the decision to count from the biggest number.	4 + = 7	3 + 4 = is calculated as 4 + 3 = 7

- read, write and interpret mathematical statements involving addition (+) and equals (=) signs
- represent and use number bonds and related addition facts within 20
- add one-digit and two-digit numbers to 20, including 0
- solve one-step problems that involve addition, using concrete objects and pictorial representations, and missing number problems such as 7 = ? + 3

	Concrete	Pictorial	Abstract
Bonds to 5, 10, 6, 7, 8 and 9	4 + 2 = 6	4+2=6	4 + 2 = ?
Adding TO + O (using bonds)	11 + 4 = 15	11 + 4 is seen as 10 + 5 = 15	
	+ =		11 + 4 =
Addition of O + O crossing boundary	8 + 9 =	8 + 9 =	
of 10	Using counters/cubes with tens frames	Drawing counters with tens frames	8+9 = 9+1+7=17
			1 7
	Leading to addition by partitioning through 10	X X X X X X X X X X X X X X X X X X X	
Use of the equals sign	e.g. 9 + 1 + 7 4 + 2 = 6	4+2=6	6 = 2 + 4
Equals is seen as a 'balance' and can	6 = 2 + 4	6 = 2 + 4	?
appear at either side of an equation.			4 2
*This is the same for all operations.*			

- recall and use addition facts to 20 fluently, and derive and use related facts up to 100
- add and subtract numbers, including:
  - a two-digit number and 1s
  - a two-digit number and 10s
  - 2 two-digit numbers
  - adding 3 one-digit numbers

	Concrete	Pictorial	Abstract
Addition of TO + O using bonds not crossing tens boundary	24 + 3 = 27	24 + 3 = 27 Drawing out counters with tens frames.	24 + 3 = 27
,	m 112		4+3=7
	+ =		20 + 7 = 27  Leading to using bonds without partitioning
			25 + 3 =
Addition of TO + 10	34 + 10 = 44	34 + 10 = 44	34 + 10 = 44
			Using bonds of 3 tens add 1 ten is 4 tens.
Addition of TO + O crossing tens	28 + 8 = 36	28 + 8 = 36	
boundary		28 + 8 = 28 + 2 + 6	28 + 8 = 36 2 6

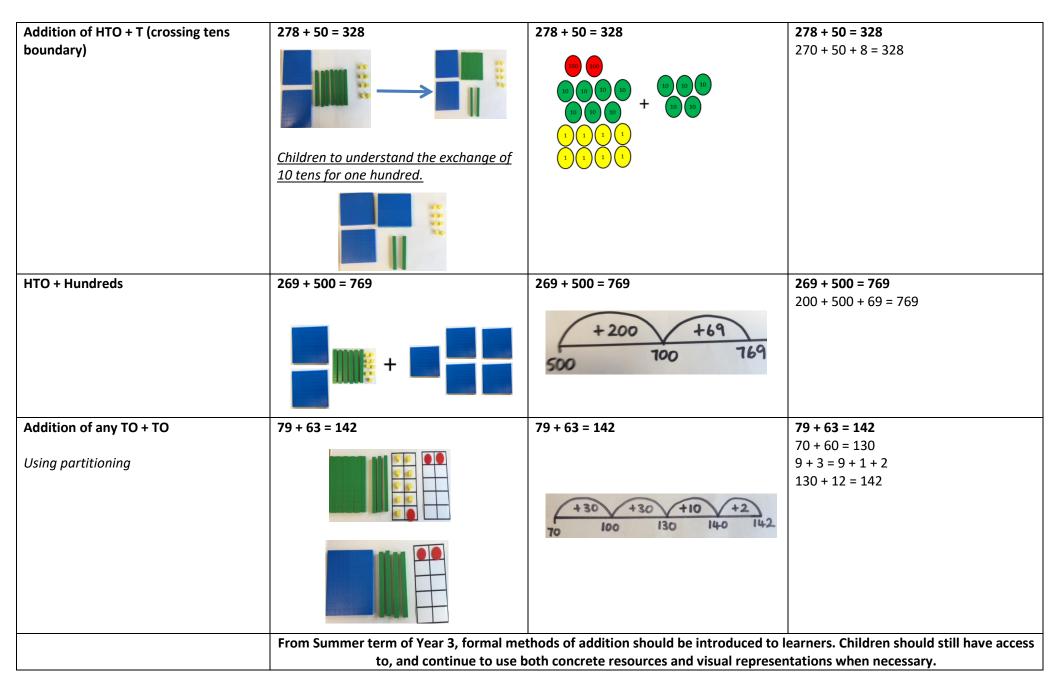
Multiple of 10 + multiple of 10 using bonds	40 + 30 = 70	40 + 30 = 70	40 + 30 = 70
bonds	+	111111	Using bonds without images.
	Using knowledge of 4 + 3 = 7		
Addition of any TO + multiples of 10	36 + 20 = 56	36 + 20 = 56	36 + 20 = 56
		::    ::	Using bond of 30 + 20 = 50 then add 6.
Addition of three single digits	6 + 2 + 4 = 12	6 + 2 + 4 = 12	6+2+4=10+2=12
Making decisions using bonds and doubles knowledge		6+2+4=12	10 Using doubles knowledge 3 + 5 + 5 = 10 + 3
			10
Addition of any TO + TO (within 100)	25 + 26 = 51	25 + 26 = 51	<b>25 + 26 = 51</b> 20 + 20 = 40
			5+6=11 $40+11=51$ Leading on to adjusting to make a multiple
			of 10. 25 + 26 = 51 30 + 21 = 51

'Never settle for less than your best'

#### Pupils should be taught to:

- add numbers with up to 3 digits, using formal written methods of columnar addition
- solve problems, including missing number problems, using number facts, place value, and more complex addition
- add numbers mentally, including:
  - a three-digit number and 1s
  - a three-digit number and 10s
  - a three-digit number and 100s

	Concrete	Pictorial	Abstract
Addition of HTO + O (using bonds)	123 + 5 = 128	123 + 5 = 128 100 10 10 + 1 1 1 1 1 1	123 + 5 = 120 + 8
Addition of HTO + O (crossing tens boundary)	125 + 8 = 133	125 + 8 = 133 125   130   133	125 + 8 = 133 125 + 5 + 3 = 133
Addition of HTO + T (using bonds)	250 + 20 = 270	250 + 20 = 270  100 100	250 + 20 = 200 + 70  Leading to any HTO + multiple of 10 (not crossing the ten boundary)  234 + 30 = 200 + 60 + 4



Addition of two numbers (up to three digits) using columnar addition	358 + 24 = 382	268 + 179 = 447
Expanded vertical method	+ 3 5 8 - 2 4 - 1 2 - 7 0 - 3 0 0 - 3 0 0 - 3 8 2	
Exceeding children may begin to use the formal columnar method.	487 + 256 = 743	
Addition of two numbers (up to three digits) using columnar addition	4 8 7	2 6 8 + <u>1 7 9</u>
Formal column method	+ 2 5 6	1 7 1 3 0
	7 4 3	3 0 0 4 4 7

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- add numbers with up to 4 digits using the formal written methods of columnar addition where appropriate
- estimate and use inverse operations to check answers to a calculation
- solve addition two-step problems in contexts, deciding which operations and methods to use and why

Add a multiple of 1000 or 100 to a 4-digit number	1700 + 1400	1800 + 700 1700 + 1400
1800 + 700		200 500 1100 + 300
Calculate mentally		1376 + 1598
<ul> <li>rounding up/down and adjusting</li> <li>doubling</li> <li>adding near doubles</li> <li>using number bond knowledge</li> </ul>		1374 + 2 1374 + 1600
Add numbers to one decimal place 1.8 + 0.7	1.8 + 0.7	1.8 + 0.7 0.2 0.5
Add numbers using columnar where necessary		
		$ \begin{array}{cccccccccccccccccccccccccccccccccccc$

- add whole numbers with more than 4 digits, including using formal written methods (columnar addition)
- add numbers mentally with increasingly large numbers
- solve addition and subtraction multi-step problems in contexts, deciding which operations and methods to use and why

Use of mental methods, where appropriate	Children should be taught to complete mental calculations by:  - rounding up/down and adjusting  - doubling  - adding near doubles  - using number bond knowledge  - adding without bridging 1, 10, 100 or 1000	Examples  1445 + 2999  1445 + 3000 - 1  1299 + 1299  Double 1300 - 2
	Use mixed decimal and whole (9 + 1.9) Used mixed decimal 1dp and 2dp (1.82 + 0.3, 1.5 + 0.07)	443 + 445 Near double 443 + 2 12.36 + 5.24 0.36 + 0.24 = 0.6 17 + 0.6 = 17.6 36.25 + 23.43
Addition of two numbers (more than four digits) using columnar addition	Formal method (using carrying) with more than four digits	Add each place value column individually  Use formal method to solve two-step problems in contexts.
Formal method	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$

Pupils should be taught to:

- perform mental calculations, using increasingly large numbers
- use their knowledge of the order of operations to carry out calculations involving the 4 operations
- solve addition multi-step problems in contexts, deciding which methods to use and why
- solve problems involving addition

Use of mental methods, where	Children should be taught to complete mental calculations by:	Examples
appropriate	<ul><li>rounding up/down and adjusting</li><li>doubling</li></ul>	1745 + 2999
	- adding near doubles	1745 + 3000 – 1
	<ul> <li>using number bond knowledge</li> </ul>	1743 + 3000 - 1
	- adding without bridging 1, 10, 100 or 1000	1399 + 1399
	- adding without bridging 1, 10, 100 or 1000	Double 1400 - 2
		Double 1400 - 2
	Use mixed wholes	1343 + 1345
	Use mixed whole and decimals	Near double 1343 + 2
	Use mixed decimals up to 3 dp	
		12.36 + 5.24
		0.36 + 0.24 = 0.6
		17 + 0.6 = 17.6
		36.25 + 23.43
		Add each place value column individually
Apply both mental and formal methods		
to solve calculations	$6 + 7 \times 8 = 62$ because multiplication first then addition when there number	are no brackets as long as the symbol moves with the
	<b>2780 – 910 + 1220</b> can be reordered to 2780 + 1220 – 910= 3090	
	Use rules of BIDMAS	

## **SUBTRACTION**

## **EYFS**

Maths ELG: Automatically recall (without reference to rhymes, counting or other aids) number bonds up to 5 (including subtraction facts) and some number bonds to 10, including double facts. Verbally count beyond 20, recognising the pattern of the counting system. Compare quantities up to 10 in different contexts, recognising when one quantity is greater than, less than or the same as the other quantity. Explore and represent patterns within numbers up to 10, including evens and odds and double facts.

	Concrete	Pictorial	Abstract
Subtract one less from a given number	4-1=3 Take one thing away	4-1=3	4 - 1 = What is one less than 4?
Count out a given number and subtract an amount	5 – 3 = 2  Take two things away	5 – 3 = 2	5-3=
Count back from a given amount	5 – 3 = 2  Count out 5 things and count back 1, 2, 3. Then count the remaining objects.	3 2 1	5 - 3 = 5 - 5 - 5 - 5 - 5 - 5 - 5 - 5 - 5 - 5

- read, write and interpret mathematical statements involving subtraction (–) and equals (=) signs
- represent and use number bonds and related subtraction facts within 20
- subtract one-digit and two-digit numbers to 20, including 0
- solve one-step problems that involve subtraction, using concrete objects and pictorial representations, and missing number problems such as 7 = ? 9

	Concrete	Pictorial	Abstract
Bonds to 5, 6, 7, 8, 9, 10	6-2=4	6-2=4	6 -2 = 6 4 ?
Subtracting TO – O (using bonds)	15 - 4 = 11 - =	15 - 4 = 11	15 – 4 =
Subtracting TO – O crossing the boundary of 10	12 – 4 = Using counters/cubes with tens frames  Leading to subtraction by partitioning through 10 e.g. 12 – 2 – 2 = 8	12 - 4 =	12-4= 2 2 12-2-2=8

#### Pupils should be taught to:

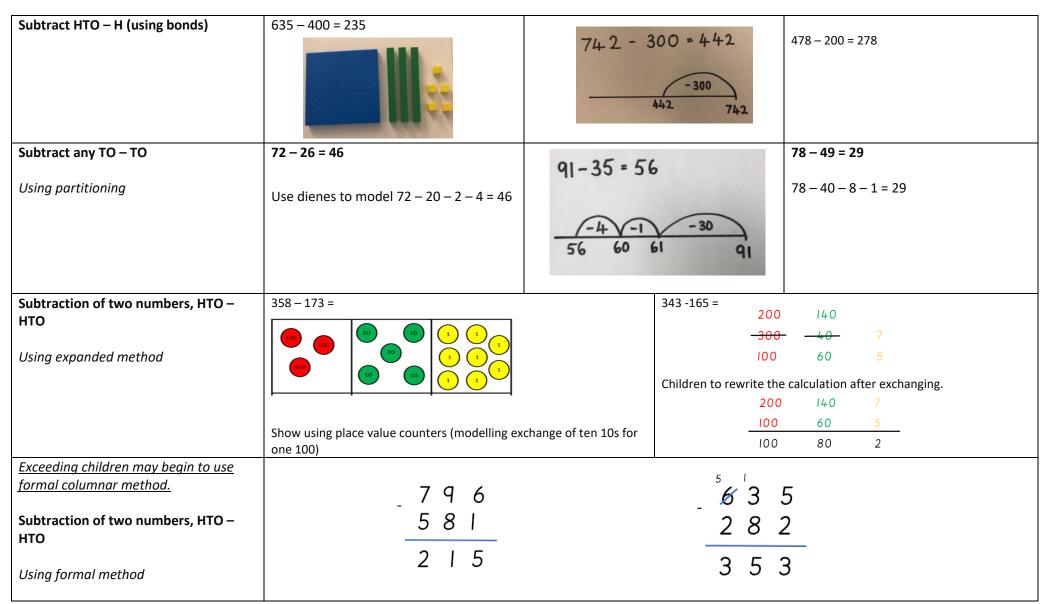
- recall and use subtraction facts to 20 fluently, and derive and use related facts up to 100
- subtract numbers using concrete objects, pictorial representations, and mentally, including:
  - a two-digit number and 1s
  - a two-digit number and 10s
  - 2 two-digit numbers
  - adding 3 one-digit numbers

	Concrete	Pictorial	Abstract
Subtraction of TO – O using bonds not crossing tens boundary	27 - 3 = 24	27 – 3 = 24 Drawing out counters with tens frames	27 - 3 = 24
			7 - 3 = 4
			20 + 4 = 24
			Leading to using bonds without partitioning
			25 - 3 =
Subtraction of TO – O crossing the	32 – 5 =	32 -5 =	
boundary (partitioning the single digit)	Model exchanging a ten for 10 ones.	Draw out on tens frames.	32 – 5 =
			2 3

Subtract TO - 10	34 - 10 = 24	34 – 10 = 24	34 – 10 = 24
			Using bonds of 3 – 1 = 2
Multiple of T – Multiple of T (using	50 – 30 =	50 – 30 =	50 20 D
bonds)			50 – 30 = Using bonds 70 – 30 = 40 because 7 – 4 = 3
Subtract from any TO – multiple of T	Take away 3 tens 56 – 30 =	56 – 30 =	
Subtract from any 10 - mattiple of 1	Take away 3 tens		56 – 30 =  Using bonds 76 – 20 = 56 because 7 – 2 = 5
Subtraction of TO -TO (using bonds)	78 – 34 =  Take three tens and four ones away	78 - 34 =	78 - 34 = 44 because 7 - 3 = 4 and 8 - 4 = 4 95 - 43 = 52 because 9 - 4 = 5 and 5 - 3 = 2
Subtract any TO – TO	72 – 26 =	91-35 = 56	78 – 49 = 29
Using partitioning	Use dienes to model 72 – 20 – 2 – 4 = 46	56 60 61 q1	78 - 40 - 8 - 1 = 29

- subtract numbers mentally, including:
  - a three-digit number and 1s
  - a three-digit number and 10s
  - a three-digit number and 100s
- subtract numbers with up to 3 digits, using formal written methods of columnar addition and subtraction
- solve problems, including missing number problems, using number facts, place value, and more complex subtraction

	Concrete	Pictorial	Abstract
Subtract HTO – O (using bonds leading to partitioning)	135 – 2 = 133	132-8=124	148 - 5 = 143 152 - 7 = 152 - 2 - 5 = 145
Subtract HTO – T (using bonds leading to partitioning)	135 – 20 = 115	0.1.5 (0 - 185	248 – 20 = 228
		245 - 60 = 185 $-20 - 40$ $185 = 205 = 245$	162 - 70 = 92 162 - 60 = 102 102 - 10 = 92



Children should also be taught to calculate the difference when two numbers are close in range e.g. 114 - 98, counting on 98 + 2 = 100 then 100 + 14 = 114, therefore the difference is 16.

- subtract numbers with up to 4 digits using the formal written methods of columnar subtraction where appropriate
- estimate and use inverse operations to check answers to a calculation
- solve subtraction two-step problems in contexts, deciding which operations and methods to use and why

Subtraction of multiples 10/100/1000	2600 - 800	2600 – 800 or 2600 – 800 = 2600 – 1000 + 200
Use of mental methods, where appropriate	Children should be taught to complete mental calculations by:  - rounding up/down and adjusting - counting up - using number bond knowledge - subtracting without bridging 1, 10, 100 or 1000	Example 532 - 199 532 - 200 + 1 308 - 289 = 19 (found by 1 + 10 + 8) 289 + 1 + 10 + 8 = 308 507 - 57 507 - 7 - 50 5839 - 1725 Subtract each column individually using place value knowledge
Subtract a pair of numbers to 1 dp	2.4 – 0.6	2.4 – 0.6 0.4 0.2
Learners should have a solid understanding of expanded method of subtraction (Year 3)  Subtraction of two numbers (up to four digits) using columnar subtraction  Formal method	Formal method (using borrowing) with numbers up to four digits.	Leading to using columnar method to solve problems using decimals up to 2 places. $ \begin{array}{cccccccccccccccccccccccccccccccccc$

- subtract whole numbers with more than 4 digits, including using formal written methods (columnar subtraction)
- subtract numbers mentally with increasingly large numbers
- solve subtraction multi-step problems in contexts, deciding which methods to use and why

Use of mental methods, where appropriate	Children should be taught to complete mental calculations by:  - rounding up/down and adjusting  - counting up  - using number bond knowledge  - subtracting without bridging 1, 10, 100 or 1000  (including decimals)  Use mixed decimal and whole (9 – 1.9)	Examples  4532 - 1999  4532 - 2000 + 1  £10 - £7.71 = £2.29  £7.71 + 29p = £8 + £2 = £10
	Used mixed decimal 1dp and 2dp (1.52 – 0.3, 1.5 – 0.07)	2507 – 57 2507 – 7 – 50 75839 – 41725 8.67 – 0.6 = 8.07 Subtract each column individually using place value knowledge
Subtraction of two numbers (more than four digits) using columnar subtraction	Formal method (using borrowing) with numbers up to four digits.	Using formal method to solve two-step problems in contexts, including decimals.
Formal method	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	£ 23 1 • 2 7 £ 1 4 • 8 1 £ 1 6 • 4 6

- perform mental calculations, including with increasingly large numbers
- use their knowledge of the order of operations to carry out calculations involving the 4 operations
- solve subtraction multi-step problems in contexts, deciding which methods to use and why
- solve problems using subtraction

Use of mental methods, where appropriate	Children should be taught to complete mental	Examples
	calculations by:	74532 – 19996
	<ul> <li>rounding up/down and adjusting</li> </ul>	74532 – 20000 + 4
	- counting up	
	<ul> <li>using number bond knowledge</li> </ul>	£10 - £7.71 = £2.29
	<ul> <li>subtracting without bridging 1, 10, 100 or 1000 (including decimals)</li> </ul>	£7.71 + 29p = £8 + £2 = £10
	,	308 – 289 = 19 (found by 1 + 10 + 8)
		289 + 1 + 10 + 8 = 308
	Use mixed wholes	
	Use mixed whole and decimals	2507 – 57
	Use mixed decimals up to 3 dp	2507 – 7 – 50
		75839 – 41725
		7.57 - 0.07 = 7.5
		6.982 - 0.08 = 6.902
		Subtract each column individually using place value knowledge
-		numbers, solving multi-step problems and applying se with a different number of decimal places)
Apply both mental and formal methods to		
solve calculations	See addition section for BIDMAS rules.	

## **MULTIPLICATION**

## **EYFS**

Maths ELG: Explore and represent patterns within numbers up to 10, including evens and odds, double facts and how quantities can be distributed equally.

	Concrete	Pictorial	Abstract
Begin to count in 2s	Count objects in pairs/groups of 2.	Use pictures of groups of 2. Model counting them.	Children to write counting sequences.
Some children may also begin to count in 5s and 10s.			2, 4, 6, 8, 10

## Year 1

## Pupils should be taught to:

• solve one-step problems involving multiplication, by calculating the answer using concrete objects, pictorial representations and arrays with the support of the teacher

	Concrete	Pictorial	Abstract
Count in 2s, 5s and 10s	Count objects in pairs/groups of 2/5/10.	Use pictures of objects in pairs/groups of 2/5/10.	2, 4, 6, 8, , 12, 14, , 15, 20, , 30, 35, , 45 30, 40, , 60, , 80, 90

- recall and use multiplication facts for the 2, 5 and 10 multiplication tables, including recognising odd and even numbers
- calculate mathematical statements for multiplication within the multiplication tables and write them using the multiplication (x) and equals (=) signs
- solve problems involving multiplication, using materials, arrays, repeated addition, mental methods, and multiplication facts, including problems in contexts

Use mathematical language with children e.g. factor, multiple, product.	Concrete	Pictorial	Abstract
Count in 3s	Count objects in groups of 3.	Use pictures of objects in groups of 3.	3, 6, 9, 12, , 18, 21,
Recall and use facts for 2, 5 and 10  Children to learn using anchor facts	Count objects in groups (2, 5 and 10)	Use images to show facts of 2, 5 and 10  2 2 2 2 2 2 2 1	2 X 5 = use facts to show inverse 5 X 2 = 10 10 ÷ 2 = 5 10 ÷ 5 = 2 2 is a factor of 10 5 is a factor of 10 10 is a multiple of 2 and 5
Children recognise that '2 x 6' is 2 multiplied 6 times or 6 lots of 2 or (repeated addition) 2 + 2 + 2 + 2 + 2 + 2. '2 is the multiplicand and 6 is the multiplier.' An awareness should be shown the 2 x 6 and 6 x 2 will give the same answer.	2 x 6	2 x 6 2 2 2 2 2 2 2 2 2 2 2 + 2 + 2 + 2 + 2 + 2 + 2 + 2 + 2 + 2 +	2 x 6 = 12 2 + 2 + 2 + 2 + 2 + 2 = 12

- recall and use multiplication facts for the 3, 4 and 8 multiplication tables
- write and calculate mathematical statements for multiplication using the multiplication tables that they know, including for two-digit numbers times one-digit numbers, using mental and progressing to formal written methods
- solve problems, including missing number problems, involving multiplication, including positive integer scaling problems and correspondence problems in which n objects are connected to m objects

	Concrete	Pictorial	Abstract
Count in 4s, 8s, 50s and 100s	Count objects in groups of 4s, 8s, 50s and 100s.	Use pictures of objects in groups of 4, 8, 50 and 100.	12, 16, 20, , 28, , 36
Recall and use facts for 3, 4 and 8  Children to learn using anchor facts	Count objects in groups (3, 4 and 8)  E.g. use matchsticks to make triangles and count in 3s.	Use images to show facts of 3, 4 and 8  3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3	3 X 4 = use facts to show inverse 4 X 3 = 12 12 ÷ 4 = 3 12 ÷ 3 = 4 3 is a factor of 12 4 is a factor of 12 12 is a multiple of 3 and 4
Multiply TO X O (O only 2, 3, 4, 5, 8)	13 X 4 = X 10 3 40 + 12 = 52 4 4 0 12	24 X 4 = 2 4 × 4 8 0 1 6 9 6	24 X 4 = 24 X 4

- recall multiplication facts for multiplication tables up to  $12 \times 12$
- use place value, known and derived facts to multiply mentally, including: multiplying by 0 and 1; multiplying together 3 numbers
- recognise and use factor pairs and commutativity in mental calculations
- multiply two-digit and three-digit numbers by a one-digit number using formal written layout
- solve problems involving multiplying and adding, including using the distributive law to multiply two-digit numbers by 1 digit, integer scaling problems and harder correspondence problems such as n objects are connected to m objects

	Concrete	Pictorial	Abstract
Count in 25s, 250s and 1000s	Count objects in 25s, 250s and 1000s.	Use pictures of objects/values to count in 25s, 250s and 1000s.	25, 50, 75, , 125,
Recall and use facts for 7, 9, 11 and 12  Children to learn using anchor facts	Count objects in groups (7, 9, 11 and 12)	Use images to show facts of 7, 9, 11 and 12	7 X 6 = use facts to show inverse 6 X 7 = 42 42 ÷ 6 = 7 42 ÷ 7 = 6 6 is a factor of 42 7 is a factor of 42 42 is a multiple of 6 and 7
Multiply a given number by 10 and 100	This objective is covered in the topic of fracti	ons.	

Multiply TO X O (grid method)  All methods to be taught alongside each other.	X 8				X	1 4 7 7 0 2 1 9 1	34 × 6  180 24
Multiply HTO X O (grid method)					Х	1 2 4	
	X	200	30	7	X	6	(145) x 8
	8	1600	240	56		6 0 0	
All methods to be taught alongside each other.						1 2 0	800
						2 4	320
						7 4 4	

#### Pupils should be taught to:

- multiply numbers up to 4 digits by a one- or two-digit number using a formal written method, including long multiplication for two-digit numbers
- multiply numbers mentally, drawing upon known facts
- multiply whole numbers and those involving decimals by 10, 100 and 1,000
- solve problems involving multiplication, including using their knowledge of factors and multiples, squares and cubes
- solve problems involving multiplication including understanding the meaning of the equals sign

Before any formal methods of multiplication are taught, the following objectives should be covered using BMS resources;

- Identify multiples and factors
- Prime, square, cube and common
- Multiplying by 10, 100 and 1000
- Know and apply facts (6 X 7 = 42 used to calculate  $0.6 \times 0.7 = 0.42$ )

Multiply 4dgt X 1dgt	x 4 1 3 4 7	x 4 1 3 4
Recap previous methods taught, expected children should be introduced to the formal method in	2 8	7
summer term of Year 5.	2   0	28938
	7 0 0	
	28000	
	28938	

Multiply 2dgt X 2dgt	Used to model place value to ensure secure		
	understanding when using expanded method	8 4	2
		x 2 7	8 4
	X 80 4		× 2 7
		2 8	
	<b>20</b> 1600 80	5 6 0	5 8 8
		8 0	1,680
	<b>7</b>   560   28		
			2 2 6 8
		2 2 6 8	
		2 2 3 3	
Multiply up to 4dgt X 2dgt			
	2 1	,	2 X 3
	6 K		X X 2
	x 386	X	6 5 4 9
	3 7	^	4 3
			4 3
	2 7 0 2	1	9647
	11,580	26	1, 9, 60
			1 1 5
	1 4 2 8 2	28	1607

- multiply multi-digit numbers up to 4 digits by a two-digit whole number using the formal written method of long multiplication
- perform mental calculations, including with mixed operations and large numbers
- use their knowledge of the order of operations to carry out calculations involving the 4 operations
- solve problems involving multiplication

Multiply 4dgt X 2dgt	2 X 3	
	x x z	
	x 6549	
	4 3	
	1 9 6 4 7	
	26,1,9,60	
	281607	
Multiply 1dgt (up to two decimal places)	~ ~	
X whole number	2 5	
	1 • 2 7	
	X	
Use this method to solve problems	^ 8	
involving various units of measure (e.g.		
money, capacity etc.)	1 0 1 (	
	10.16	

## **DIVISION**

## **EYFS**

Maths ELG: Explore and represent patterns within numbers up to 10, including evens and odds, double facts and how quantities can be distributed equally.

	Concrete	Pictorial	Abstract
Begin to count in 2s  Some children will also count in 5s and	Count objects in pairs/groups of 2.	Use pictures of groups of 2. Model counting them.	Children to write counting sequences.
10s.			2, 4, 6, 8, 10

## Year 1

#### Pupils should be taught to:

• solve one-step problems involving division, by calculating the answer using concrete objects, pictorial representations and arrays with the support of the teacher

	Concrete	Pictorial	Abstract
Count in 2s, 5s and 10s	Count objects in pairs/groups of 2/5/10.	Use pictures of objects in pairs/groups of 2/5/10.	2, 4, 6, 8, , 12, 14, 15, 20, , 30, 35, , 45
Children develop an understanding of division as both grouping and sharing	Share out objects between two people. Group objects into groups of 5/10	Share between 2 people. How many groups of 2?	Pencils are in packs of 5. How many packs do I need for 15 pencils? I share 15 pencils between 5 people. How many pencils each?

- recall and use division facts for the 2, 5 and 10 multiplication tables, including recognising odd and even numbers
- calculate mathematical statements for division within the multiplication tables and write them using the division (÷) and equals (=) signs
- solve problems involving division, using materials, arrays, repeated addition, mental methods, and division facts, including problems in contexts

	Concrete	Pictorial	Abstract
Recall and use facts for 2, 5 and 10  Children to learn using anchor facts	Count objects in groups (2, 5 and 10)	Use images to show facts of 2, 5 and 10  2 2 2 2 2 2 2	2 X 5 = use facts to show inverse 5 X 2 = 10 10 ÷ 2 = 5 10 ÷ 5 = 2 2 is a factor of 10 5 is a factor of 10 10 is a multiple of 2 and 5
Children develop an understanding of division as both grouping and sharing	Grouping/ sharing sheet Use of manipulatives	Shows 6 groups of 3 Shows 3 groups of 6	18 pencils are shared equally amongst 6 children. How many each? 18 pencils are put into packets of 6. Howmany in each packet?

- recall and use division facts for the 3, 4 and 8 multiplication tables
- write and calculate mathematical statements for division using the multiplication tables that they know, including for two-digit numbers times one-digit numbers, using mental and progressing to formal written methods
- solve problems, including missing number problems, involving division, including positive integer scaling problems and correspondence problems in which n objects are connected to m objects

	Concrete	Pictorial	Abstract
Recall and use facts for 3, 4 and 8  Children to learn using anchor facts	Count objects in groups (3, 4 and 8)	Use images to show facts of 3, 4 and 8  3 3 3 3 3  3 3 3 3	3 X 4 = use facts to show inverse 4 X 3 = 12 12 ÷ 4 = 3 12 ÷ 3 = 4 3 is a factor of 12 4 is a factor of 12 12 is a multiple of 3 and 4
Division TO ÷ O (2, 3, 4, 5, 8, 10)  Including remainders	72 ÷ 3 = 24	72 ÷ 4	17 ÷ 4 = 4 r

- recall division facts for multiplication tables up to  $12 \times 12$
- use place value, known and derived facts to divide mentally
- recognise and use factor pairs and commutativity in mental calculations
- multiply two-digit and three-digit numbers by a one-digit number using formal written layout
- solve problems involving multiplying and adding, including using the distributive law to multiply two-digit numbers by 1 digit, integer scaling problems and harder correspondence problems such as n objects are connected to m objects

	Concrete	Pictorial	Abstract
Recall and use facts for all numbers 2-12  Children to learn using anchor facts	Count objects in groups (7, 9, 11 and 12)	Use images to show facts of 7, 9, 11 and 12  7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7	7 X 6 = use facts to show inverse 6 X 7 = 42 42 ÷ 6 = 7 42 ÷ 7 = 6 6 is a factor of 42 7 is a factor of 42 42 is a multiple of 6 and 7
Division TO ÷ O  Including remainders	24 ÷ 7 = 3 r 3	74 ÷ 6 = 12 · 2	43 ÷ 7 = 6 r

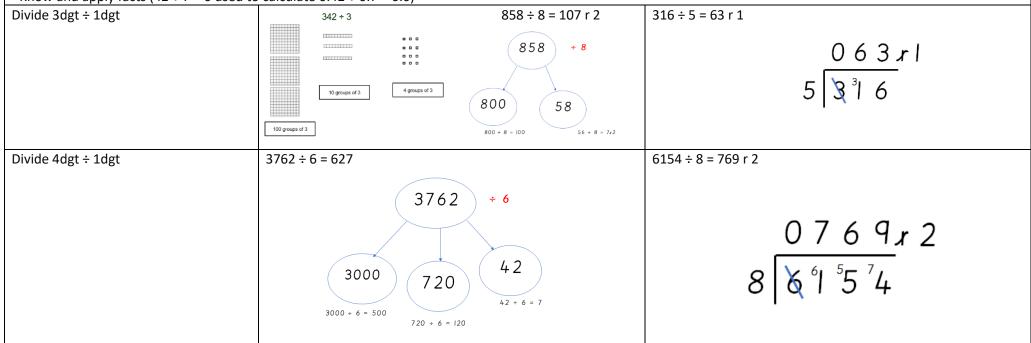
#### Pupils should be taught to:

- divide numbers mentally, drawing upon known facts
- divide numbers up to 4 digits by a one-digit number using the formal written method of short division and interpret remainders appropriately for the context
- divide whole numbers and those involving decimals by 10, 100 and 1,000
- solve problems involving division, including using their knowledge of factors and multiples, squares and cubes
- solve problems involving addition, subtraction, multiplication and division and a combination of these, including understanding the meaning of the equals sign
- solve problems involving division, including scaling by simple fractions and problems involving simple rates

Before any formal methods of division are taught, the following objectives should be covered using resources;

- Identify multiples and factors
- Prime, square, cube and common
- Dividing by 10, 100 and 1000

- Know and apply facts  $(42 \div 7 = 6 \text{ used to calculate } 0.42 \div 0.7 = 0.6)$ 



- divide numbers up to 4 digits by a two-digit whole number using the formal written method of long division, and interpret remainders as whole number remainders, fractions, or by rounding, as appropriate for the context
- divide numbers up to 4 digits by a two-digit number using the formal written method of short division where appropriate, interpreting remainders according to the context
- perform mental calculations, including with mixed operations and large numbers
- use their knowledge of the order of operations to carry out calculations involving the 4 operations
- solve problems involving division

Division of 3dgt ÷ 2dgt	493 ÷ 15 = 32 r 13	493 ÷ 15 = 32 r 13
	493 450 + 15 = 30 43 + 15 = 2 \$13	$ \begin{array}{r} 3 \ 2x \   \ 3 \\ 15 \ 4 \ 9 \ 3 \\ \underline{450} \\ 43 \\ \underline{30} \\ 1 \ 3 \end{array} $
Division of 4dgt ÷ 2dgt	8943 ÷ 22 = 406 r 11  8943	8943 ÷ 22 = 406 r 11  4 0 6 r      22 8 9 4 3  8 8 0 0    4 3    1 3 2
Division of 3 and 4 digit numbers by a 2 digit number		42 84 126 0 2 2 0 r 4 148 42 9 9 2 8 4 4